

On estimates of solutions of the non-stationary  
Stokes problem in anisotropic Sobolev spaces and on  
estimates for the resolvent of the Stokes operator

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