As is to be expected in view of (4.39) the boundary integral gives after evaluation of the sums

$$(6.26)\qquad \oint = \oint_{\partial\Omega} \mu^{-\beta}(a^{11}a^{22}-(a^{12})^2)\,(v_y dv_x - v_x dv_y) \quad .$$

By the way (4.43) was derived in the present case we come to (6.13).

The proof of (6.14) follows the same lines. Of course the formulae become somehow lengthy but there are no additional difficulties.

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